$Math\ 2263\ Section\ 10\ Quiz\ 8$

Time limit: 15 minutes

 ${f 1.}$ (4 points) The joint density function for a pair of random variables X and Y is

$$f(x,y) = \begin{cases} 4xy & \text{if } 0 \le x \le 1, \ 0 \le y \le 1, \\ 0 & \text{otherwise.} \end{cases}$$

Find the expected value of X.

2. (5 points) Write down an integral in polar coordinates that yields the surface area of the part of the paraboloid $z = 9 - x^2 - y^2$ that lies above the xy-plane. Do not evaluate the integral.

 $\mathbf{3.}$ (6 points) Evaluate the iterated integral

$$\int_0^2 \int_0^{2z} \int_0^{\ln x} x e^{-y} dy dx dz.$$